

MESSAGES OF THIS TALK

1. Our exploration of phases of QCD matter relies on a precise method of hadron abundance analysis within the SHARE statistical hadronization model.
2. Irrespective of how a common QCD phase - the QGP state was created at SPS, RHIC, *and* LHC and how it evolves to hadronization, we observe in the final state the same physical conditions of the fireball particle source.
3. These properties of the QGP fireball are derived from what we see in all emitted hadronic particles.
4. Given universal hadronization conditions we realize that when QGP hadronizes it evaporates into free-streaming hadrons.
5. Many orders of magnitude of particle yields are described solely by: i) volume changes; and ii) strangeness content change from system to system and as function of centrality.
6. Consequence: there is no interlaced 'phase' of hadrons, no afterburners in general needed, nor are these in any way consistent with experimental results at LHC.

QCD PHASES STUDIED BY MEANS OF HADRON PRODUCTION

February 17, 2014 Wroclaw



Dedicated to Ludwik Turko on occasion of his 70'th birthday

Key References:

JR and Jean Letessier
Critical hadronization pressure,
J.Phys. G **36** (2009) 064017

arXiv:0902.0063 and 0901:2406

Michal Petran and JR
Universal hadronization condition. . .,

Phys. Rev C **88** 021901(R) (2013);

arXiv:1303.0913



Michal Petran, Jean Letessier, Vojtech Petracek and JR *Hadron production and QGP hadronization . . .*, Phys. Rev. C **88**, 034907 (2013); arXiv:1303.2098

OUTLINE: QUARK KITCHEN

1. SHM Description of particle production in HI experiments
2. QGP fireball physical properties at break-up
3. Universal Hadronization Conditions



STATISTICAL HADRONIZATION MODEL (SHM)

- Assuming equal hadron production strength irrespective of produced hadron type
- Particle yields depend only on available phase space
 - Micro-canonical – Fermi model
fixed energy and number of particles
E. Fermi, Prog.Theor.Phys. 5 (1950) 570
 - Canonical – fixed number of particles, average energy: T
 - Grand-canonical + average number of particles:
 $\mu \Leftrightarrow \Upsilon = e^{(\mu/T)}$
- Exploration of source properties in particle co-moving frame – collective matter flow irrelevant

PARTICLE ABUNDANCES

- Experiments report average particle abundances over many collision events
- Model calculations to describe an average event

TO DESCRIBE PRODUCED HADRON YIELDS

- Average per collision yield of hadron i is calculated from integral of the distribution over phase space

$$\begin{aligned}\langle N_i \rangle &\rightarrow \frac{dN_i}{dy} = g_i \frac{dV}{dy} \int \frac{d^3p}{(2\pi)^3} n_i; \quad n_i(\varepsilon_i; T, \gamma_i) = \frac{1}{\gamma_i^{-1} e^{\varepsilon_i/T} \pm 1} \\ &= \frac{g_i T^3}{2\pi^2} \frac{dV}{dy} \sum_{n=1}^{\infty} \frac{(\pm 1)^{n-1} (\gamma_i)^n}{n^3} \left(\frac{nm_i}{T} \right)^2 K_2 \left(\frac{nm_i}{T} \right)\end{aligned}$$

- | | |
|---------------------------------------|--|
| • Hadron mass | PDG Tables |
| • Degeneracy (spin), $g_i = (2J + 1)$ | PDG Tables |
| • Overall normalization | outcome of SHM fit |
| • Hadronization temperature | outcome of SHM fit |
| • Fugacity γ_i for each hadron | – see next slide
outcome of SHM fit |

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- **Hadron mass**

PDG Tables

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FUGACITY AND QUARK FLAVOR CHEMISTRY

FLAVOR CONSERVATION FACTOR

$$\lambda_q = e^{\mu/T}$$

- controls difference between quarks and antiquark of same flavor $q - \bar{q}$
- “Relative”** chemical equilibrium

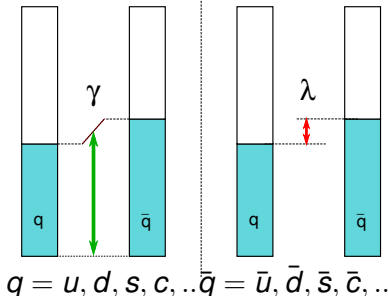
FLAVOR YIELD FACTOR γ_q

- phase spaces occupancy: absolute abundance of flavor q
- controls number of $q + \bar{q}$ pairs
- “Absolute”** chemical equilibrium

P. Koch, B. Müller, JR, *Strangeness in Relativistic Heavy Ion Collisions*
Phys. Reports 142 (1986) 167-262

OVERALL FUGACITY $\Upsilon = \gamma\lambda$

- product of constituent quark flavor Υ_i
- example: $\Lambda(uds)$ ($q = u, d$)
 $\Upsilon_{\Lambda(uds)} = \gamma_q^2 \gamma_s \lambda_q^2 \lambda_s$
 $\Upsilon_{\bar{\Lambda}(\bar{u}\bar{d}\bar{s})} = \gamma_q^2 \gamma_s \lambda_q^{-2} \lambda_s^{-1}$



HADRON RATIOS — CONCEPTUAL TEST OF SHM

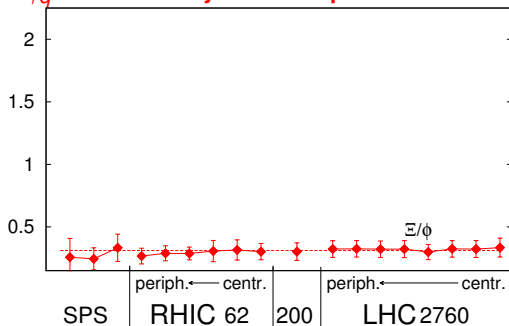
few(er)SHM parameters, easy to compare with data:

$$\frac{\Xi}{\phi} \equiv \sqrt{\frac{\Xi^-(ssd) \Xi^+(\bar{s}\bar{s}\bar{d})}{\phi(s\bar{s}) \phi(s\bar{s})}} = \sqrt{\frac{\gamma_s^4 \gamma_q^2 \lambda_s^2 \lambda_q \lambda_s^{-2} \lambda_q^{-1}}{\gamma_s^4 \lambda_s^2 \lambda_s^{-2}}} \frac{V_{\Xi}}{V_{\phi}} f(T, m_{\Xi}, m_{\phi})$$

$$= \gamma_q f(T, m_{\Xi}, m_{\phi}).$$

$\gamma_q = 1$ and system dependent **T IMpossible**
 $\gamma_q \simeq 1.6$ and system INdependent **T $\simeq 140$ perfect**

OTHER RATIOS



$$\frac{\phi}{\pi} \propto \frac{\gamma_s^2}{\gamma_q^2}$$

$$\frac{\Xi}{\pi} \propto \frac{\gamma_s^2}{\gamma_q}$$

$$\frac{\phi}{K} \propto \frac{\gamma_s}{\gamma_q}$$

$$\frac{\Xi}{K} \propto \gamma_s$$

- Ratios $\propto \gamma_s$ change
 $\Rightarrow \gamma_s$ change

HADRON RATIOS — CONCEPTUAL TEST OF SHM

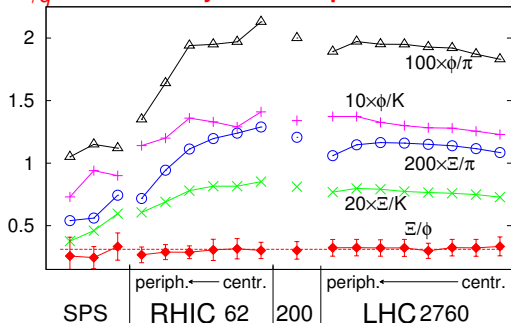
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OTHER RATIOS



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$$\frac{\Xi}{K} \propto \gamma_s$$

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 $\Rightarrow \gamma_s$ change

STANDARDIZED PROGRAM TO FIT SHM PARAMETERS

Statistical HAdronization with REsonances: (SHARE)

- SHM implementation in publicly available program
Giorgio Torrieri et al, Arizona + Krakow; SHAREv1 (2004),
SHAREv2 + Montreal, added fluctuations (2006)
Michal Petran SHARE with CHARM: (2013)

SHARE INCORPORATES MANY THOUSANDS LINES OF CODE

- Hadron mass spectrum > 500 hadrons (PDG 2012)
- Hadron decays > 2500 channels (PDG 2012)
- Integrated hadron yields, ratios and decay cascades
- OUT: Experimentally observable $\lesssim 30$ hadron species
- AND: Physical properties of the source at hadronization
– also as input in fit e.g. constraints: $Q/B \simeq 0.39$, $\langle s - \bar{s} \rangle = 0$

PROCEDURE – FITTING SHM PARAMETERS TO DATA

1. Input: $T, V, \gamma_q, \gamma_s, \lambda_q, \lambda_s, \lambda_3$
2. Compute yields of **all hadrons**
3. Decay feeds
– particles experiment observes
4. Compare to exp. data (χ^2)
5. Including bulk properties, constraints
6. Tune parameters to match data (minimize χ^2)

Particle list (> 500 states)

LIQUID $n = 1$ MEMBERS	GAS $n = 2$ MEMBERS	STRANGE
π^+	π^0	AT
π^-	η	AT
$\omega(782)$	$\eta(548)$	$\pi^0(137)$
$\pi^0(137)$	$\eta(940)$	$\pi^0(1405)$
$\pi^0(1450)$	$\eta(959)$	$\pi^0(1470)$
$\pi^0(1500)$	$\eta(1300)$	$\pi^0(1500)$
$\pi^0(1640)$	$\eta(1370)$	$\pi^0(1640)$
$\pi^0(1670)$	$\eta(1405)$	$\pi^0(1670)$
$\pi^0(1700)$	$\eta(1450)$	$\pi^0(1700)$
$\pi^0(1770)$	$\eta(1530)$	$\pi^0(1770)$
$\pi^0(1820)$	$\eta(1640)$	$\pi^0(1820)$
$\pi^0(1875)$	$\eta(1680)$	$\pi^0(1875)$
$\pi^0(1900)$	$\eta(1700)$	$\pi^0(1900)$
$\pi^0(1950)$	$\eta(1760)$	$\pi^0(1950)$
$\pi^0(1975)$	$\eta(1820)$	$\pi^0(1975)$
$\pi^0(2000)$	$\eta(1875)$	$\pi^0(2000)$
$\pi^0(2025)$	$\eta(1900)$	$\pi^0(2025)$
$\pi^0(2050)$	$\eta(1950)$	$\pi^0(2050)$
$\pi^0(2075)$	$\eta(2000)$	$\pi^0(2075)$
$\pi^0(2100)$	$\eta(2050)$	$\pi^0(2100)$
$\pi^0(2125)$	$\eta(2100)$	$\pi^0(2125)$
$\pi^0(2150)$	$\eta(2150)$	$\pi^0(2150)$
$\pi^0(2175)$	$\eta(2200)$	$\pi^0(2175)$
$\pi^0(2200)$	$\eta(2250)$	$\pi^0(2200)$
$\pi^0(2225)$	$\eta(2300)$	$\pi^0(2225)$
$\pi^0(2250)$	$\eta(2350)$	$\pi^0(2250)$
$\pi^0(2275)$	$\eta(2400)$	$\pi^0(2275)$
$\pi^0(2300)$	$\eta(2450)$	$\pi^0(2300)$
$\pi^0(2325)$	$\eta(2500)$	$\pi^0(2325)$
$\pi^0(2350)$	$\eta(2550)$	$\pi^0(2350)$
$\pi^0(2375)$	$\eta(2600)$	$\pi^0(2375)$
$\pi^0(2400)$	$\eta(2650)$	$\pi^0(2400)$
$\pi^0(2425)$	$\eta(2700)$	$\pi^0(2425)$
$\pi^0(2450)$	$\eta(2750)$	$\pi^0(2450)$
$\pi^0(2475)$	$\eta(2800)$	$\pi^0(2475)$
$\pi^0(2500)$	$\eta(2850)$	$\pi^0(2500)$
$\pi^0(2525)$	$\eta(2900)$	$\pi^0(2525)$
$\pi^0(2550)$	$\eta(2950)$	$\pi^0(2550)$
$\pi^0(2575)$	$\eta(3000)$	$\pi^0(2575)$
$\pi^0(2600)$	$\eta(3050)$	$\pi^0(2600)$
$\pi^0(2625)$	$\eta(3100)$	$\pi^0(2625)$
$\pi^0(2650)$	$\eta(3150)$	$\pi^0(2650)$
$\pi^0(2675)$	$\eta(3200)$	$\pi^0(2675)$
$\pi^0(2700)$	$\eta(3250)$	$\pi^0(2700)$
$\pi^0(2725)$	$\eta(3300)$	$\pi^0(2725)$
$\pi^0(2750)$	$\eta(3350)$	$\pi^0(2750)$
$\pi^0(2775)$	$\eta(3400)$	$\pi^0(2775)$
$\pi^0(2800)$	$\eta(3450)$	$\pi^0(2800)$
$\pi^0(2825)$	$\eta(3500)$	$\pi^0(2825)$
$\pi^0(2850)$	$\eta(3550)$	$\pi^0(2850)$
$\pi^0(2875)$	$\eta(3600)$	$\pi^0(2875)$
$\pi^0(2900)$	$\eta(3650)$	$\pi^0(2900)$
$\pi^0(2925)$	$\eta(3700)$	$\pi^0(2925)$
$\pi^0(2950)$	$\eta(3750)$	$\pi^0(2950)$
$\pi^0(2975)$	$\eta(3800)$	$\pi^0(2975)$
$\pi^0(3000)$	$\eta(3850)$	$\pi^0(3000)$
$\pi^0(3025)$	$\eta(3900)$	$\pi^0(3025)$
$\pi^0(3050)$	$\eta(3950)$	$\pi^0(3050)$
$\pi^0(3075)$	$\eta(4000)$	$\pi^0(3075)$
$\pi^0(3100)$	$\eta(4050)$	$\pi^0(3100)$
$\pi^0(3125)$	$\eta(4100)$	$\pi^0(3125)$
$\pi^0(3150)$	$\eta(4150)$	$\pi^0(3150)$
$\pi^0(3175)$	$\eta(4200)$	$\pi^0(3175)$
$\pi^0(3200)$	$\eta(4250)$	$\pi^0(3200)$
$\pi^0(3225)$	$\eta(4300)$	$\pi^0(3225)$
$\pi^0(3250)$	$\eta(4350)$	$\pi^0(3250)$
$\pi^0(3275)$	$\eta(4400)$	$\pi^0(3275)$
$\pi^0(3300)$	$\eta(4450)$	$\pi^0(3300)$
$\pi^0(3325)$	$\eta(4500)$	$\pi^0(33$

Decay tree (>2500 channels)

Ω^- DECAY MODES

Mode	Fraction (Γ_i/Γ)	Confidence level
$F_1: \Lambda K^-$	$187 \pm 0.7\%$	
$F_2: \Sigma^0 \pi^-$	$228 \pm 0.7\%$	
$F_3: \Xi^- \pi^0$	$8.6 \pm 0.4\%$	
$F_4: \Xi^- \pi^+ \pi^-$	$(1.31^{+0.04}_{-0.03}) \times 10^{-4}$	
$F_5: \Xi^0 \pi^- \pi^0$	$< 7 \times 10^{-5}$	90%
$F_6: \Xi^0 \pi^- \pi^+ \pi^-$	$(5.6 \pm 2.8) \times 10^{-3}$	
$F_7: \Xi^- \gamma$	$< 4.6 \times 10^{-4}$	90%

$\Delta S = 2$ forbidden (S^2) modes

$F_8: \Lambda \pi^- \pi^0$	$52 < 2.9 \times 10^{-6}$	90%
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SHM computation:

1. calculate particle yields
2. decay unstable particles
3. compare to experimental data, calculate χ^2

$$\chi^2 = \sum_{i=1}^N \frac{(f_{i,\text{theory}} - f_{i,\text{experiment}})^2}{(\Delta f_{i,\text{systematic}} + \Delta f_{i,\text{statistical}})^2}$$

Tune parameters
to minimize χ^2

Output:
Hadron yields, ratios
Physical properties

Experimental data:
integrated yield of
several hadron
species, π , K , p , Λ , ϕ

(AGS) SPS – FIXED TARGET

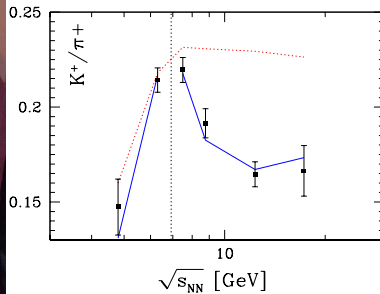
Does SHM describe particle production at SPS?

Is there any characteristic physical property of the hadronizing
QGP fireball?

Table 1: AGS (on left) and SPS energy range particle multiplicity data sets used in fits (see text). In bottom of table, we show the fitted statistical parameters and the corresponding chemical potentials.

$E[4\text{GeV}]$	11.6	20	30	40	80	158
$\sqrt{s_{NN}} [\text{GeV}]$	4.84	6.26	7.61	8.76	12.32	17.27
y_{CM}	1.6	1.88	2.08	2.22	2.57	2.91
$N_{4\pi}$ centrality	most central	7%	7%	7%	7%	5%
N_W , AGS: p/π^+	1.23 ± 0.13	349 ± 6	349 ± 6	349 ± 6	349 ± 6	362 ± 6
Q/b	0.39 ± 0.02	0.394 ± 0.02	0.394 ± 0.02	0.394 ± 0.02	0.394 ± 0.02	0.39 ± 0.02
$(s - \bar{s})/(s + \bar{s})$	0 ± 0.05	0 ± 0.05	0 ± 0.05	0 ± 0.05	0 ± 0.05	0 ± 0.05
π^+	133.7 ± 9.9	190.0 ± 10.0	241 ± 13	293 ± 18	446 ± 27	619 ± 48
π^- , AGS: π^-/π^+	1.23 ± 0.07	221.0 ± 12.0	274 ± 15	322 ± 19	474 ± 28	639 ± 48
K^+ , AGS: K^+/K^-	5.23 ± 0.5	40.7 ± 2.9	52.9 ± 4.2	56.1 ± 4.9	73.4 ± 6	103 ± 10
K^-	3.76 ± 0.47	10.3 ± 0.3	16 ± 0.6	19.2 ± 1.5	32.4 ± 2.2	51.9 ± 4.9
ϕ , AGS: ϕ/K^+	0.025 ± 0.006	1.89 ± 0.53	1.84 ± 0.51	2.55 ± 0.36	4.04 ± 0.5	8.46 ± 0.71
Λ	18.1 ± 1.9	27.1 ± 2.4	36.9 ± 3.6	43.1 ± 4.7	50.1 ± 10	44.9 ± 8.9
$\bar{\Lambda}$	0.017 ± 0.005	0.16 ± 0.05	0.39 ± 0.06	0.68 ± 0.1	1.82 ± 0.36	3.68 ± 0.55
Ξ^-		1.5 ± 0.3	2.42 ± 0.48	2.96 ± 0.56	3.8 ± 0.87	4.5 ± 0.20
Ξ^+			0.12 ± 0.05	0.13 ± 0.03	0.58 ± 0.19	0.83 ± 0.04
$\Omega + \bar{\Omega}$, or K_S				0.14 ± 0.07		81 ± 4
$V[\text{fm}^3]$	3649 ± 331	4775 ± 261	2229 ± 340	1595 ± 383	2135 ± 235	3055 ± 454
$T [\text{MeV}]$	153.5 ± 0.8	151.7 ± 2.8	123.8 ± 3	130.9 ± 4.4	135.2 ± 0.01	136.0 ± 0.01
$\lambda_{q,HP}^*$	5.21 ± 0.07	3.53 ± 0.09	2.86 ± 0.09	2.42 ± 0.09	1.98 ± 0.07	1.744 ± 0.02
λ_{HP}^*	1.565^*	1.39 ± 0.05	1.45 ± 0.05	1.34 ± 0.06	1.25 ± 0.18	1.155 ± 0.03
$\gamma_{q,HP}^*$	0.366 ± 0.008	0.49 ± 0.03	1.54 ± 0.37	1.66 ± 0.14	1.65 ± 0.01	1.64 ± 0.01
γ_{HP}^*	0.216 ± 0.009	0.40 ± 0.03	1.61 ± 0.07	1.62 ± 0.25	1.52 ± 0.06	1.63 ± 0.02
$\lambda_{B,HP}^*$	0.875 ± 0.166	0.877 ± 0.05	0.935 ± 0.013	0.960 ± 0.027	0.973 ± 0.014	0.975 ± 0.005
$\mu_B [\text{MeV}]$	759	574	390	347	276	227
$\mu_S [\text{MeV}]$	180	141	83.7	77.6	62.0	56.0

PARTICLE YIELDS DESCRIBED, HORN TRACKED PERFECTLY

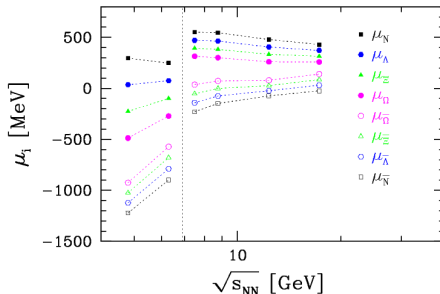
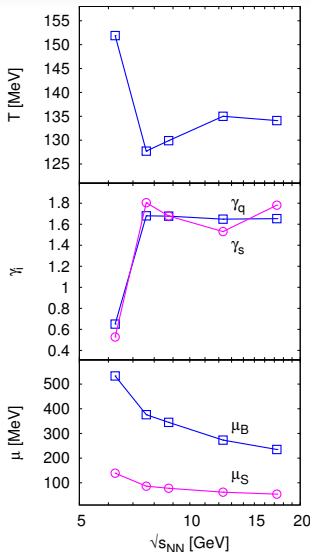


SHM PARAMETERS NA49-SPS

LOWEST $\sqrt{s_{NN}} = 6.26$ GeV
OFTEN STANDS OUT

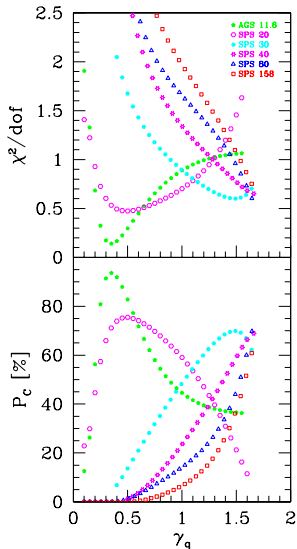
beginning at $\sqrt{s_{NN}} = 7.61$ features
different

- T increases with $\sqrt{s_{NN}}$
- $\gamma_q \rightarrow$ condensation limit $\simeq 1.6$
- Chemical potentials:



JR, J.Letessier, *Critical Hadronization Pressure*, J.Phys. G36 (2009) 064017 JR,
J.Letessier, *Particle Production and Deconfinement Threshold*, arXiv 0901.2406

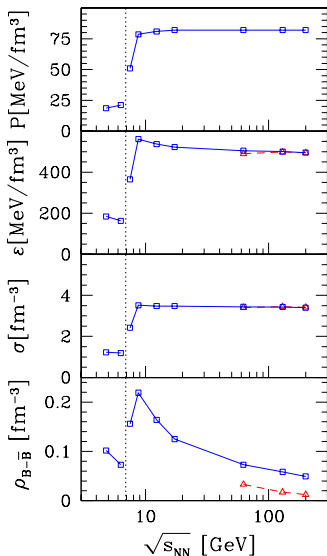
IS CHEMICAL NON-EQUILIBRIUM JUSTIFIED AT AGS/SPS?



- Top AGS and lowest SPS energy: χ^2 -minimum at $\gamma_q < 1$, change to $\gamma_q = 1.6$ between $\sqrt{s_{NN}} = 6.26$ and 7.61 GeV
- P [%] – confidence level satisfactory for best fit, while $\gamma_q = 1$ often not acceptable.

UNIVERSAL HADRONIZATION SPS – RHIC

AGS – SPS – RHIC
red RHIC central y

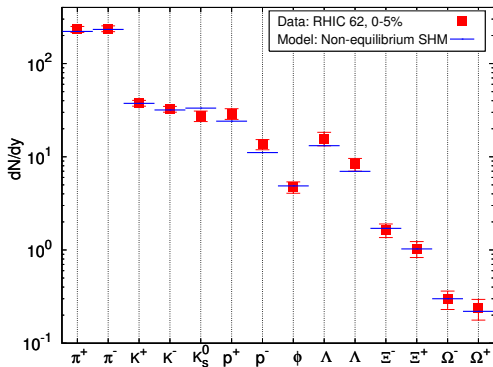


- P , ϵ , σ all show clearly common hadronization condition
- Baryon density peaks beyond the reaction mechanism change between $\sqrt{s_{NN}} = 6.26, 7.61$ GeV.

UNIVERSAL HADRONIZATION AT RHIC-62 AS FUNCTION OF CENTRALITY

For how small a system is the physical property of the
hadronizing QGP fireball universal?

SHM AT RHIC 62 WORKS FOR US



SHM results: Petran et al., Acta Phys.Polon.Supp. 5 (2012) 255-262
Data from: [STAR Collaboration], Phys.Rev.C79, 034909 (2009)
[STAR Collaboration], Phys.Rev.C79, 064903 (2009).

MODEL PARAMETERS

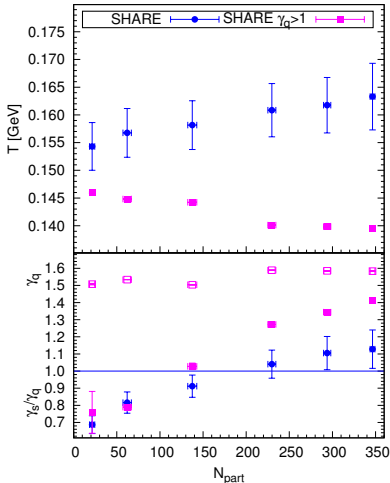
- $T = 140 \text{ MeV}$
- $dV/dy = 850 \text{ fm}^3$
- $\gamma_q = 1.6$
- $\gamma_s = 2.2$
- $\lambda_q = 1.16$
- $\lambda_s = 1.05$
- $\Rightarrow \mu_B = 62.8 \text{ MeV}$
- $\chi^2/ndf = 0.38$

PHYS. PROPERTIES

- $\varepsilon = 0.5 \text{ GeV/fm}^3$
- $P = 82 \text{ MeV/fm}^3$
- $\sigma = 3.3 \text{ fm}^{-3}$

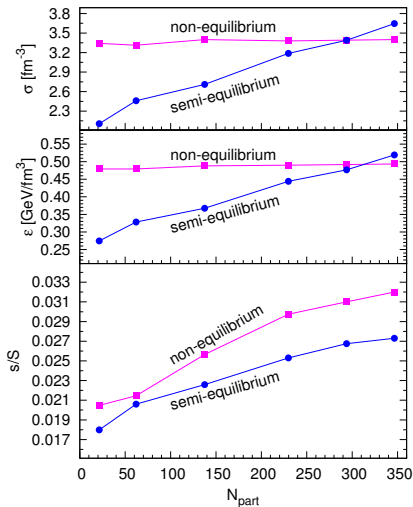
RHIC 62 GeV ACROSS CENTRALITY:

TWO APPROACHES (SEMI)EQUILIBRIUM $\gamma_q = 1$ AND
'NONEQUILIBRIUM' $\gamma_q \neq 1$ QGP BREAKUP



- Au–Au collisions at $\sqrt{s_{NN}} = 62.4$ GeV at RHIC
- $\pi, K, p, \phi, \Lambda, \Xi$ and Ω fitted across centrality
- $\gamma_s \neq 1$ necessary to describe multistrange particles $\Rightarrow$ excludes chemical equilibrium
- $\gamma_s > 1$ in central collisions – strangeness overpopulation

PHYSICAL PROPERTIES AT RHIC 62 GEV



Non-equilibrium result $\gamma_q \neq 1$:
universal hadronization

AND: SAME PHYSICAL
CONDITIONS AS AT SPS FOR ALL
RHIC-62 CENTRALITIES

- Entropy density
 $\sigma = 3.3 \text{ fm}^{-3}$
- Energy density
 $\varepsilon = 0.5 \text{ GeV}/\text{fm}^3$
- Critical pressure
 $P = 82 \text{ MeV}/\text{fm}^3$
- s/S near chemical
equilibrium QGP
 $s/S \simeq 0.03$

M. Petran et al., Acta Phys. Polon. Supp. 5 (2012) 255-262

$dV/dy|_{central} = 17 \times dV/dy|_{peripheral}$

IMPORTANCE OF STRANGENESS/ENTROPY=PARTICLE MULTIPLICITY

s/S : ratio of number of active degrees of freedom in QGP

For chemical equilibrium:

$$\frac{s}{S} \simeq \frac{1}{4} \frac{n_s}{n_s + n_{\bar{s}} + n_q + n_{\bar{q}} + n_G} = \frac{\frac{g_s}{2\pi^2} T^3 (m_s/T)^2 K_2(m_s/T)}{(g 2\pi^2/45) T^3 + (g_s n_f/6) \mu_q^2 T} \simeq \frac{1}{35} = 0.0286$$

with $\mathcal{O}(\alpha_s)$ interaction $s/S \rightarrow 1/31 = 0.0323$

CENTRALITY A, and/or ENERGY DEPENDENCE:

Chemical non-equilibrium QGP occupancy of strangeness γ_s^Q

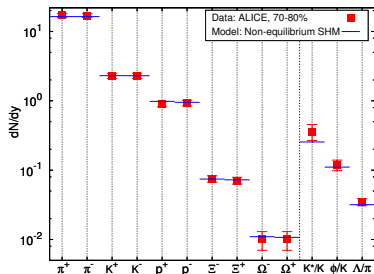
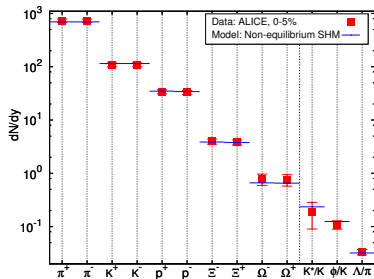
$$\frac{s}{S} = \frac{0.03 \gamma_s^Q}{0.4 \gamma_G + 0.1 \gamma_s^Q + 0.5 \gamma_q^Q + 0.05 \gamma_q^Q (\ln \lambda_q)^2} \rightarrow 0.03 \gamma_s^Q.$$

LHC – $45\times$ HIGHER ENERGY (THAN RHIC 62)

Does SHM describe particle production at LHC?

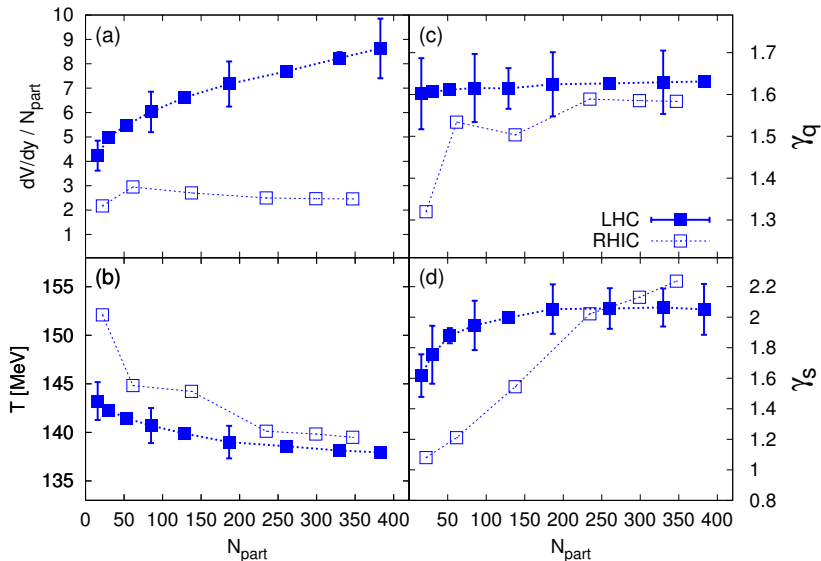
Does the QGP fireball hadronizes at the same ‘universal’
hadronization conditions as at SPS and RHIC 62?

FIT TO LHC HADRON YIELDS WORKS PERFECTLY and nearly same parameters as RHIC 62

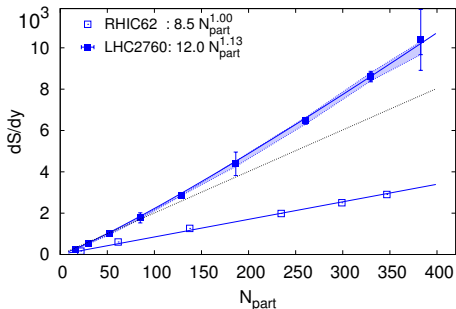


- Data from:
Pb–Pb at $\sqrt{s_{NN}} = 2.76$ TeV
- Non-equilibrium SHM describes data across centrality
- Hadron yield range spans 5 orders of magnitude from central to peripheral

MODEL PARAMETERS AT LHC COMPARED TO RHIC

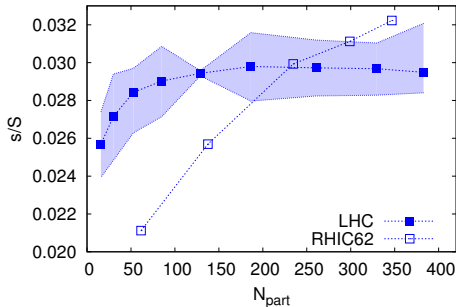


IMPORTANT DIFFERENCES: ENTROPY, STRANGENESS VS. CENTRALITY



M.Petran et al., Phys. Rev. C 88, 034907 (2013)

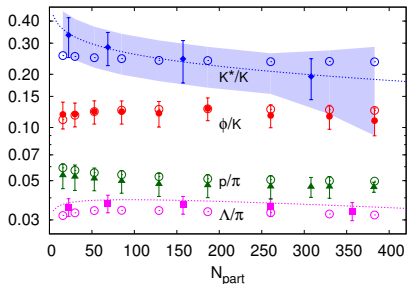
- LHC – steeper than linear
- Additional centrality dependent entropy production



M.Petran et al., Phys. Rev. C 88, 034907 (2013)

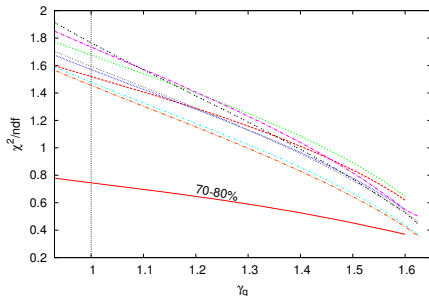
- For small N_{part} rapid increase of strangeness
- For large N_{part} steady level of strangeness

PRECISE DATE DEMANDS CHEMICAL NON-EQUILIBRIUM OF LIGHT u, d AND STRANGE s QUARKS, $\gamma_i \neq 1$



M.Petran et al., Phys. Rev. C 88, 034907 (2013)

- $\frac{p(uud)}{\pi(ud)} \propto \gamma_q$
- $\frac{p(uud)}{\pi(ud)} \simeq 0.05 \Rightarrow \gamma_q \simeq 1.6$

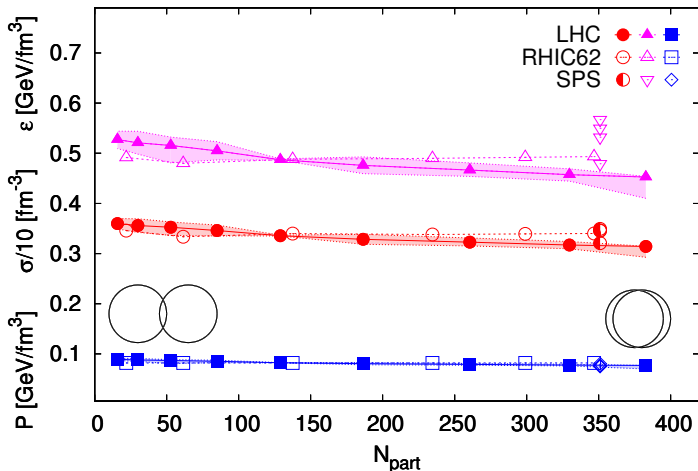


M.Petran et al., Phys. Rev. C 88, 034907 (2013)

- $\gamma_q = 1$ no special importance
- $4\times$ smaller χ^2 for $\gamma_q = 1.6$

Only non-equilibrium describes all LHC data
afterburners ruin centrality systematics

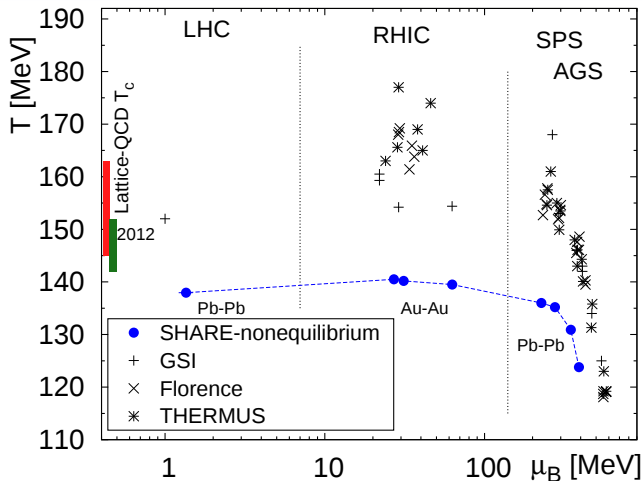
UNIVERSAL HADRONIZATION CONDITIONS: RHIC vs LHC AS FUNCTION OF CENTRALITY + SPS POINTS



M.Petran et al., Phys. Rev. C 88, 021901(R) (2013)

M.Petran et al., Phys. Rev. C 88, 034907 (2013)

CONSISTENCY WITH LATTICE-QCD



We need to remember that HI collisions are highly dynamic and observed phase boundary MUST be below lattice results.

MESSAGES OF THIS TALK: 1. WE ARE BEST FRIENDS.



2. Irrespective of how a common QCD phase - the QGP state was created at SPS, RHIC, *and* LHC and how it evolves to hadronization, we observe in the final state the same physical conditions of the fireball particle source – with varying V and s .
4. Given universal hadronization conditions we realize that when QGP hadronizes it evaporates into free-streaming hadrons.